

Math 142(1)

Name: \_\_\_\_\_

Spring 2015

Exam #3

5/11/2015

Time Limit: 75 Minutes

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You may *not* use your books or notes on this exam. You are required to show your work on each problem on this exam. The following rules apply:

- **Organize your work**, in a reasonably neat and coherent way, in the space provided. Work scattered all over the page without a clear ordering will receive very little credit.
- **Mysterious or unsupported answers will not receive full credit.** A correct answer, unsupported by calculations, explanation, or algebraic work will receive no credit; an incorrect answer supported by substantially correct calculations and explanations might still receive partial credit.
- If you need more space, use the back of the pages; clearly indicate when you have done this.

Grade Table (for teacher use only)

Question	Points	Score
1	20	
2	20	
3	20	
4	20	
5	0	
Total:	80	

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1. (20 points) Sketch the region enclosed by the given curves. Find its area.

$$y = 12 - x^2 \quad y = x^2 - 6$$

2. (20 points) Find the volume of a cone with height  $H$  and base radius  $R$ . (*Hint: rotate an appropriate line around the  $y$  axis*)

3. (20 points) Find the volume of the solid obtained by rotating about the  $y$ -axis the region bounded by  $y = 2x^2 - x^3$  and  $y = 0$ .

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4. (20 points) Find an arc-length function for  $y^2 = 4(x + 4)^3$  starting at point  $(0, \sqrt{32})$ . Find the length of the curve from  $x = 0$  to  $x = 3$ .

5. (20 points) Find the solution of the differential equation

$$\frac{dy}{dx} = \frac{\ln(x)}{xy}$$

with initial condition  $y(1) = 2$ .